

**S.R. Fatepuria College**  
**Class Test Examination- 2020**  
**Semester- 4, Paper- CC-T-08**  
**Subject-Mathematics(Honours)**

**F.M. – 10**

**Time- 30 Minutes**

**1) Answer any two questions :-      2x1= 2**

- a) State the first Mean Value theorem of integral calculus.
- b) State the necessary condition for Riemann integral of a function.
- c) State the Cauchy condition for uniform convergence of sequence of real valued function on a set E.

**2) Answer any two questions :-      2x4= 8**

- a) Let  $f$  be a real-valued function on the closed interval  $[a,b]$  and  $P$  be any partition of  $[a,b]$ . Define upper integral sum  $U(P,f)$  and lower integral sum  $L(P,f)$  and obtain the definitions of the upper and lower Riemann integrals of  $f$  on  $[a,b]$ .
- b) State and prove Darboux theorem.
- c) Show that every function continuous on a closed interval is Riemann-integrable over that interval.

**Semester- 4, Paper- CC-T-10**  
**Subject-Mathematics(Honours)**

**F.M. – 10**

**Time- 30 Minutes**

**1) Answer any two questions :-      2x1= 2**

- a) Give an example of a finite integral domain.
- b) Is  $(2\mathbb{Z}, +, \cdot)$  is a commutative ring with unity ?
- c) Give the definition of divisors of zero.

**2) Answer any one question :- 1x2= 2**

- a) If a ring  $R$  contains a left divisor ( or a right divisor ) or zero , prove that  $R$  contains a both sided divisor of zero.
- b) In a ring  $(R, +, \cdot)$  show that
  - (i)  $a \cdot 0 = 0 \cdot a = 0$
  - (ii)  $a(-b) = (-a) \cdot b = -(a \cdot b)$  for all  $a, b$  in  $R$ .

**3) Answer any two questions :- 3x2= 6**

- a) Prove that a finite integral domain is a field.
- b) The cancelation law holds in a ring  $R$  if and only if  $R$  has no divisor of zero.
- c) Let  $R$  be finite ring with  $n$  elements and  $S$  be a subring of  $R$  containing  $m$  elements. Prove that  $m$  is a divisor of  $n$ .